The Research Grants Council of Hong Kong NSFC/RGC Joint Research Scheme <u>Joint Completion Report</u>

(Please attach a copy of the completion report submitted to the NSFC by the Mainland researcher)

Part A: The Project and Investigator(s)

1. Project Title

On Mathematical Theory of the Compressible Fluid-dynamical Equations

2. Investigator(s) and Academic Department/Units Involved

	Hong Kong Team	Mainland Team
Name of Principal Investigator <i>(with title)</i>	Professor Zhouping XIN	Professor Hai-liang LI
Post	William M. W. Mong Professor of Mathematics	Professor
Unit / Department / Institution	The Institute of Mathematical Sciences, CUHK	Capital Normal University, China
Contact Information	zpxin@ims.cuhk.edu.hk	hailiang_li@cnu.edu.cn
Co-investigator(s) (with title and institution)	/	Professor Chengchun HAO

3. **Project Duration**

	Original	Revised	Date of RGC/ Institution Approval
			(must be quoted)
Project Start date	1 January 2015	/	
Project Completion date	31 December 2018	/	
Duration (in month)	48	/	
Deadline for Submission of Completion Report	30 September 2019	/	

Part B: The Completion Report

5. Project Objectives

- 5.1 Objectives as per original application
 - 1. Well-posedness and behaviors of the compressible Navier-Stokes system
 - 2. Well-posedness and vacuum problem of the compressible Euler Equations
 - 3. Asymptotical behaviors of the Vlasov-Poisson (Maxwell)-Boltzmann system
- 5.2 Revised Objectives

Date of approval from the RGC:

Reasons for the change: _

(N/A)

6. Research Outcome

Major findings and research outcome *(maximum 1 page; please make reference to Part C where necessary)*

With the direct support of the joint research scheme, the PIs and their collaborators have achieved all the objectives of the project by establishing the following important results. First, we have obtained some important and surprising results on the both local and global (in time) well-posedness of strong solutions for the compressible Navier-Stokes systems. Indeed, through joint efforts, the PIs and their collaborators have discovered the surprising phenomena that there exists no finite energy classical solution with bounded entropy for the full compressible Navier-Stokes systems with compact initial density for any positive time. This implies that there is no even short time well-posedness theory in the inhomogeneous spaces for fast decaying initial density in general, which is in sharp contrast to the case of non-vacuum initial data. Stronger results without boundness of entropy have been obtained in one-dimensional case. These results imply, in particular, that the local well-posedness of strong solutions can be obtained only in homogeneous spaces in general, and the behavior of strong solutions may be extremely complex compared with the non-vacuum case. These results have been published in [8]. Then the PI from Hong Kong and his collaborators have shown the finite-time blow-up of smooth solutions, established the blow-up criteria, and gain understanding on the possible blow-up mechanism, which solved the Nash's conjecture on finite-time singularity formation which must be due to either mass concentration or over-heating. Furthermore, we first identify the self-similar scaling and used it to show that there are first-type finite time singularity for isentropic compressible Navier-Stokes system. These results have been published in [1, 2, 14, 21]. The PI from Hong Kong and his collaborators have proved the nonlinear asymptotic stability for the Lane-Emden solution for the viscous gaseous star problem with degenerate density-dependent viscosity, which is a long standing difficult problem and the result is published in [3]. We also made important progress on the global in time well-posedness and large time behavior by establishing the global strong solution with small energy but large oscillations and vacuum for both 2D and 3D isentropic Navier-Stokes systems in [16, 20] which are based on our new discovery that the pressure behaves dispersively in the presence of far field vacuum, by showing the global smooth solutions for various models of compressible Navier-Stokes system with degenerate viscosity which are reported in [17, 12], and by showing the optimal decay of strong solutions without restrictions on the lower frequency parts [13]. We have also obtained important results on the asymptotic behavior of solutions to the compressible Navier-Stokes system for large Reynolds number in the presence of either physical boundaries or interfacial boundaries with stress free boundary conditions by establishing uniform regularity estimates and obtaining vanishing viscosity limits in the general case, which are published in [4, 19] and are generalized to the incompressible cases in [18, 23]. The PI from Hong Kong and Dr. C. P. Wang discovered and rigorously proved the existence of vacuum for 2-dimensional steady isentropic compressible flow in a general expanding nozzle, which is published in [11]. Furthermore, the PI from Hong Kong and his collaborators have also obtained substantial results on transonic flows with or without shocks in general nozzles with variable sections which solve some long standing open problems in this area in [5, 9, 10, 11, 22, 25], on well-posedness of weak solutions for liquid-crystals in 2-dimensional space in [6, 7], and on global entropy weak solutions to weakly nonlinear gas dynamics [24] and large time asymptotic stability of nonlinear waves under periodic perturbations in [15]. In summary, with the support of this joint scheme, the PI from Hong Kong side and his collaborators have produced 25 research papers, out of which 19 have been published in peer-reviewed journals and 2 chapters for research monographs.

Potential for further development of the research and the proposed course of action *(maximum half a page)*

The main results and methods developed in this joint research scheme indicate great complexities of the motions of viscous compressible fluids in the presence of vacuum state. These give rises many important problems such as the analysis of the specific entropy, the necessities of investigating the vacuum interface problems compared with the non-vacuum case, the important of studying the degenerating viscosity and heat-conductivity coefficients. Such kinds of problems provide natural models for further mathematical theory of mixed and degenerate nonlinear partial differential equations. These important issues will be considered in the future researches.

7. The Layman's Summary

(describe <u>in layman's language</u> the nature, significance and value of the research project, in no more than 200 words)

This research project concerns the mathematical studies of the compressible Navier-Stokes equations and related systems which govern some of most important motions in continuum mechanics. It is found that in the presence of vacuum, the great complexities of the system give rise to many interesting new phenomena such as immediate gain of energy, finite time mass concentration and/or overheating, increasing of oscillations over vacuum, and dispersion of the pressure, etc.. By developing some new techniques and ideas, we have obtained substantial results which are not only important for physical problems such as motion of viscous gaseous stars, but also for theories on free boundary and fixed initial-boundary value problems for degenerate mixed-type systems of nonlinear partial differential equations. The ideas and methods developed here should share lights on other physical problems too.

Part C: Research Output

8. Peer-reviewed journal publication(s) arising <u>directly</u> from this research project (Please attach a copy of each publication and/or the letter of acceptance if not yet submitted in the previous progress report(s). All listed publications must acknowledge RGC's funding support by quoting the specific grant reference.)

The	e Latest Status	of Publica	tions	Author(s)	Title and	Submitted to	Attached	Acknowledge	Accessible
Year of	Year of	Under	Under	(bold the	Journal/	RGC	to this	d the support	from the
publication	Acceptance	Review	Preparation	authors	Book	(indicate the	report (Yes	of this Joint	institutional
	(For paper		_	belonging to	(with the	year ending	or No)	Research	repository
	accepted but		(optional)	the project	volume,	of the		Scheme	(Yes or No)
	not yet			teams and	pages and	relevant		(Yes or No)	
	published)			denote the	other	progress			
				corresponding	necessary	report)			
				author with an	publishing				
				asterisk*)	details				
					specified)				
[1]				Quansen Jiu,	Remarks on	2016	No	Yes	No
2015				Yuexun Wang,	blow-up of				
2015				Znouping Xin^	smooth				
					the				
					compressible				
					fluid with				
					constant and				
					degenerate				
					viscosities. J.				
					Differential				
					259(7)				
					2981-3003				
[2]				Xiangdi Huang,	On formation	2016	No	Yes	No
				Zhouping Xin*	of singularity				
2016					for				
					non-isentropic				
					Navier-Stokes				
					equations				
					conductivity				
					Discrete				
					Contin. Dyn.				
					Syst. 36(8),				
					4477-4493				

[3] 2016		Tao Luo, Zhouping Xin* , Huihui Zeng	Nonlinear asymptotic stability of the Lane-Emden solutions for the viscous	2016	No	Yes	No
			gaseous star problem with degenerate density dependent viscosities				
			Comm. Math. Phys. 347(3), 657-702				
[4] 2015		Yong Wang, Zhouping Xin* , Yan Yong	Uniform regularity and vanishing viscosity limit for the compressible	2016	No	Yes	No
			Navier-Stokes with general Navier-slip boundary conditions in three- dimensional domains. SIAM J. Math. Anal.				
[5]		Chunnana	4123-4191	2016	No	Var	No
2016		Wang, Zhouping Xin*	curves of smooth subsonic- sonic and transonic flows. SIAM J. Math. Anal. 48(4), 2414-2453	2010	110	105	110
[6] 2016		Jinkai Li, Edriss S. Titi, Zhouping Xin*	On the uniqueness of weak solutions to the Ericksen- Leslie liquid crystal model in R2. Math. Models Methods Appl. Sci., 26(4), 803-822	2016	No	Yes	No
[7]		Jinkai Li, Zhouping Xin *	Global existence of weak solutions to the non- isothermal nematic liquid crystals in 2D. Acta Math. Sci. Ser. B Engl. Ed. 36(4), 973-1014	2016	No	Yes	No

[8] 2019		Hailiang Li, Yuexun Wang, Zhouping Xin*	Non- Existence of Classical Solutions with Finite Energy to the Cauchy Problem of the Compressible Navier-Stokes Equations, ARMA, 232(2), 557-590	2016	Yes	Yes	No
נין		Zhouping Xin*	On Admissible Locations of Transonic Shock Fronts for Steady Euler Flows in an Almost Flat Finite Nozzle with Prescribed Receiver Pressure	No	Y es	res	NO
[10] 2019		Chunpeng Wang, Zhouping Xin *	On an Elliptic Free Boundary Problem and Subsonic Jet Flows for a Given Surrounding Pressure, SIAM J. Math. Anal., 51 (2), 1014-1045	No	Yes	Yes	No
[11] 2019		Chunpeng Wang, Zhouping Xin *	Smooth Transonic Flows of Meyer Type in De Laval Nozzles, Arch. Rat. Mech. Anal. 232, 1597-1647	No	Yes	Yes	No
[12]	Y	Zhouping Xin* Shengguo Zhu	Well- posedness of Three- Dimensional Isentropic Compressible Navier-Stokes Equations with Degenerate Viscosities and Far Field Vacuum	No	Yes	Yes	No
[13]		Zhouping Xin* Jiang Xu	, Optimal Decay for the Compressible Navier-Stokes Equations Without Additional Smallness Assumptions	No	Yes	Yes	No

	[14] 2019		Zhen Lei, Zhouping Xin*	On scaling invariance and type-I singularities for the compressible Navier-Stokes equations, Science China Mathematics, 62(11), 2271-2286	No	Yes	Yes	No
ļ	[15]		Zhouping Xin* , Oian Yuan	Asymptotic Stability of	No	Yes	Yes	No
	2019		Yuan Yuan	Shock Waves and Rarefaction Waves Under Periodic Perturbations For 1-D Convex Scalar Conservation Laws, SIAM J. Math. Anal. 51(4), 2021 2021				
ŀ	[16]		Iing Li	2971-2994 Global Well-	No	Ves	Vec	No
	2019		Zhouping Xin*	Posedness and Large Time Asymptotic Behavior of Classical Solutions to the Compressible Navier-Stokes Equations with Vacuum, Annals of PDE, 5(1):7, pp.37, https://doi.org /10.1007/s408 18-019-0064- 5	110	105	1 05	140
	[17] 2018		Quansen Jiu, Yi Wang, Zhouping Xin*	Global classical solutions to two- dimensional compressible Navier-Stokes equations with large data in R ² , Physica D: Nonlinear Phenomena, Vol. 376-377, 180-194	No	Yes	Yes	No
	[18]		Shijin Ding,	Stability	No	Yes	Yes	No
	2018		Quanrong Li, Zhouping Xin *	analysis for the incompressi- ble Navier-Stokes equations with Navier boundary conditions, J. Math. Fluid Mech., 20(2), 603-629				

[19] 2018		Yu Mei, Yong Wang, Zhouping Xin*	Uniform regularity for the free surface compressible NavierStokes equations with or without surface tension, Math. Models Methods Appl. Sci., 28(2), 259-336, https://doi.org /10.1142/S02 18202518500 082	No	Yes	Yes	No
[20] 2018		J. Li, Zhouping Xin*	Global existence of regular solutions with large oscillations and vacuum for compressible flows, Springer, Handbook of Math. Analysis in Mechanics of Viscous Fluids, 38, 2037-2083	No	Yes	No	No
[21] 2018		X. D. Huang, Zhouping Xin*	Finite time blow-up of regular solutions for compressible flows, Handbook of math. analysis in mechanics of viscous fluids, Springer, 40, 2183-2261	No	Yes	No	No
[22]	2019	C. P. Wang, Zhouping Xin*	Regular Subsonic- sonic Flows in General Nozzles	No	Yes	Yes	No
[23] 2017		Shu Wang, Zhouping Xin*	Boundary layer problems in the vanishing viscosity- diffusion limits for the incompressi- ble MHD system (in Chinese), Sci Sin Math, 47(10), 1303-1326, doi: 10.1360/N012 016-00211	No	Yes	Yes	No

[24]		Peng Qu,	Global	No	Yes	Yes	No
		Zhouping Xin*	entropy				
2017			solutions to				
			weakly				
			nonlinear gas				
			dynamics,				
			Adv. Math.				
			316, 292-355				

9. Recognized international conference(s) in which paper(s) related to this research project was/were delivered (Please attach a copy of each delivered paper. All listed papers must acknowledge RGC's funding support by quoting the specific grant reference.)

Month/Year/ Place	Title	Conference Name	Submitted to RGC (indicate the year ending of the relevant progress	Attached to this report (Yes or No)	Acknowledged the support of this Joint Research Scheme (Yes or No)	Accessible from the institutional repository (Yes or No)
			report)			
Dec, 2018, Taipei, Taiwan	Degenerate Potential Equation and Subsonic-Sonic Flows	The 2nd annual meeting of International Consortium of Chinese Mathematicians (ICCM) 2018	No	Yes	Yes	No
Dec, 2018, Shanghai, China	Some Results on The Prandtl Boundary Layer Equations	The Workshop on Theory of Boundary Layers and Related Topics	No	Yes	Yes	No
Sept, 2018, Chengdu, China	跨音速激波和混合 型方程	The 16th CSIAM Annual Meeting 2018	No	Yes	Yes	No
Aug, 2018, Xiamen, China	Riemann and Shock Waves Theory	Summer School on Mathematics for Graduate Students	No	Yes	Yes	No
Aug, 2018, Heilongjiang, China	Compressible Navier-Stokes Equations and Vacuum Dynamics	International Conference on Nonlinear Partial Differential Equations	No	Yes	Yes	No
Jul, 2018, Dalian, China	Riemann and Shock Waves Theory	Tianyuan Summer School	No	Yes	Yes	No
Jul, 2018, Harbin, China	Incompressible inviscid resistive MHD surface waves in 2D	16th Summer School on Nonlinear PDEs	No	Yes	Yes	No
Jul, 2018, Sichuan, China	Entropy-bounded solutions in inhomogeneous spaces to the compressible Navier-Stokes equations with vacuum	Mini-Workshop on Differential Equations	No	Yes	Yes	No
Jun, 2018, Shanghai, China	Incompressible inviscid resistive MHD surface waves in 2D	Approximately 60: An international conference on nonlinear PDEs	No	Yes	Yes	No
Jun, 2018, L'Aquila, Italy	Transonic Shocks and Mixed Type PDEs	Workshop on Mathematical Fine Structures in Fluid Dynamics	No	Yes	Yes	No
May, 2018, Hubei, China	Transonic Shocks and Mixed Type PDEs	The 3rd Workshop on Partial Differential Equations and Their Applications	No	Yes	Yes	No

May 2018	Incompressible	2018 Conference on	No	Vec	Vec	No
May, 2010,	invisaid resistive	Mathamatical Eluid	110	105	105	110
China	MHD surface	Mechanics Equations				
	waves in 2D					
May, 2018,	Free Boundaries	2018 Conference on	No	Yes	Yes	No
Guangzhou,	and Subsonic Jet	Nonlinear Partial				
China	Flows	Differential Equations				
May. 2018.	Incompressible	Mathematical Fluid	No	Yes	Yes	No
Bad Boll	inviscid resistive	Dynamics Workshop 2018	110			
Germony	MHD surface	Dynamics workshop 2010				
Germany						
	waves in 2D					27
Apr, 2018	Incompressible	NCTS Workshop on	No	Yes	Yes	No
Taipei, Taiwan	inviscid resistive	Computational				
	MHD surface	Mathematics and Applied				
	waves in 2D	Analysis				
Mar. 2018.	Transonic Shocks	Workshop on Dynamical	No	Yes	Yes	No
Kunming	in General Nozzles	System Nonlinear PDEs				
China		and Their Imaging				
Ciinia		Drocossing Applications				
2010	T '1 1	Processing Applications	27			λĭ
Mar, 2018,	Incompressible	Workshop on 2018 Medical	No	Yes	Yes	No
Guangzhou,	inviscid resistive	Imaging Analysis and				
China	MHD surface	Nonlinear PDEs				
	waves in 2D					
Jan, 2018.	On subsonic and	The 6th International	No	Yes	Yes	No
Sichuan	sonic iets	Conference of Western				
China	some jeus	Nonlinear PDFs				
Lan 2019	T	Nominear I DES	N-	V	V	No
Jan, 2018,	Transonic Shocks	Nonlinear PDEs in	No	Y es	Y es	INO
Sanya, China	in Nozzles	Continuum Mechanics and				
		Related Topics Workshop				
Jan, 2018,	Incompressible	Workshop on	No	Yes	Yes	No
Beijing, China	inviscid resistive	Mathematical Problems				
5 6,	MHD surface	in Eluid Machanias				
	waves in 2D	in Fluid Mechanics				
Iop. 2018	Transonic Shocks	Conference on applied	No	Vac	Vac	No
Jan, 2016,	in Na ==1-	A unalassia	INO	1 05	1 08	110
Jinan, China	in Nozzies	Analysis				
Dec, 2017,	Transonic Shocks	Workshop on Transonic	No	Yes	Yes	No
Xiamen, China	and Mixed-Type	Flows and PDEs				
	Equations					
Dec, 2017,	Incompressible	PDE Model and Nonlinear	No	Yes	Yes	No
Sanya, China	inviscid resistive	Waves for Fluids and				
	MHD surface	Plasma Workshop				
	waves in 2D	i incline // crincitop				
Dec. 2017	Diamann and Shock	The Workshop on Partial	No	Vac	Vac	No
Dec, 2017,		Differential E meticus for	INO	105	105	110
Guangznou,	waves Theory	Differential Equations for				
China		Young Scholars				
Dec, 2017,	跨音速激波和混合	Workshop on Partial	No	Yes	Yes	No
Jilin, China	型方程	Differential Equations				
Dec. 2017	Incompressible	Frontier of Theory and	No	Vec	Vec	No
Hong Kong	invisoid resistive	Tiontier of Theory and	110	105	105	110
Hong Kong		Applications of				
	MHD surface	Nonlinear PDEs				
	waves in 2D					
Nov, 2017	On Global	International Conference	No	Yes	Yes	No
Shanghai,	Well-Posedness of	on Analysis of Complex				
China	the 2D Prandtl's	Fluids				
	Boundary Lavers					
	Equations					
Nov 2017	On Global	Workshop on Nonlinger	No	Vac	Vac	No
$100^{\circ}, 201^{\circ}, 10^{\circ}$			INO	1 05	108	110
Nanjing, China	well-Posedness of	Partial Differential				
	the 2D Prandtl's	Equations and Their				
	Boundary Layers	Applications				
	Equations					
Nov, 2017.	Incompressible	Conference on Analysis	No	Yes	Yes	No
Xiamen, China	inviscid resistive	of Complex Fluids				
, c	MHD surface	or complex r luius				
	waves in 2D					
Sant 2017	Commerce ::-1	Workshop '11	NT-	V	V	No
Sept, 2017,	Compressible	Worksnop on compressible	INO	res	res	110
Snanghai,	INAVIER-Stokes	navier-Stokes Equations				
China	Equations and					
	Wearning Dymamics					

Sent 2017	On Global	2017Workshop on	No	Vac	Vac	No
Sept, 2017,			INO	105	105	110
Shanghai,	Well-Posedness of	Mathematical Study of				
China	the 2D Prandtl's	Boundary Layers and				
	Boundary Layers	Related Topics				
	Equations					
Sept 2017	On	The 2017 NCTS Applied	No	Ves	Ves	No
Toinoi Toiwon	Multi Dimonsional	Mathematica Workshop	110	105	103	110
Taipei, Taiwan	Multi-Dimensional	Mathematics Workshop				
	Compressible					
	Navier-Stokes					
	Systems					
Jul 2017	On Transonic	Conference on	No	Ves	Ves	No
Jurich	Shocks in Curved	Mothematics Physics and	110	105	105	
Zurien		international states, i hysics and				
	Nozzies	their Interaction				
Jul, 2017,	Transonic Shocks	The 15th Summer	No	Yes	Yes	No
Xian, China	and Mixed PDEs	School on Nonlinear				
1 1 2017) I		17	ŊŢ
Jul, 2017,	N-S万程:进展和挑	西部局校数字教师著期字	No	Yes	Yes	No
Sichuan, China	战	校				
Jun 2017	Free Boundaries	Workshop on Fluid	No	Ves	Ves	No
Jun, 2017,			INO	105	103	110
Henan, China	and Subsonic Jet	Mechanics Equations				
	Flows					
Jun, 2017,	Multi-Dimensional	Workshop on Partial	No	Yes	Yes	No
Guangzhou,	Shock Wave	Differential Equations				
China	Theory Progress	1				
China	and Challenges					
1 2017		XX 7 1 1	NT	37	X 7	N-
Jun, 2017,	Free Boundaries	Workshop on	No	Yes	Yes	NO
Shanghai,	and Subsonic Jet	Multi-Dimensional				
China	Flows	Conservation Laws				
May, 2017.	Multi-Dimensional	Workshop on Transonic	No	Yes	Yes	No
Xiamen	Shock Wave	Flow and Mixed Type				
Chino	Theory Drograss	Equations				
China	Theory: Progress	Equations				
	and Challenges					
Apr, 2017,	Free Boundaries	China-Australia Joint	No	Yes	Yes	No
Queensland,	and Subsonic Jet	Conference on Nonlinear				
Australia	Flows	PDE and Related Topics				
Apr. 2017	Ereo Doundarios	Porspectives of	No	Vac	Vac	No
Api, 2017,		respectives of	INO	1 05	1 05	110
Beijing, China	and Subsonic Jet	Mathematics in the 21st				
	Flows	Century: Conference in				
		Celebration				
		of the 90th Anniversary of				
		the Department of				
		Mathematics of Tsinghua				
		I missonaites				
		University				
Apr, 2017,	Free Boundaries	International Conference	No	Yes	Yes	No
Beijing, China	and Subsonic Jet	on PDEs - Silkroad				
	Flows	Mathematics Center Series				
		International Conference				
Mar 2017	Free Boundaries	The 1th PDEs Youth	No	Ves	Ves	No
Cuanazhau	and Subsania Ist	Eamine	110	103	103	110
Guangzhou,	and Subsome Jet	Forum				
China	Flows					
Feb, 2017,	Periodic Motions	Conference on Applied	No	Yes	Yes	No
Jinan, China	for	Analysis				
	One-Dimensional	-				
	Nonlinear Gas					
	Dynamics Systems					
D 2016	Dynamics Systems		N		17	Ŋ
Dec, 2016,	Periodic Motions	Workshop on Partial	No	Yes	Yes	No
Wuhan, China	for	Differential Equations and				
	One-Dimensional	their Applications				
	Nonlinear Gas					
	Dynamics Systems					
Dec. 2016	Clabal Endetance of	Washelsen en DDE-	2016	No	V	No
Dec, 2016	Global Existence of	workshop on PDEs	2016	INO	res	INO
Nanjing, China	Weak Solutions to					
	the Barotropic					
	Compressible					
	Navier-Stokes					
	Flows with					
	Degenerate					
1	Vigoosition					
1	v iscosities					

Nov, 2016 Xian, China	Nonlinear Asymptotic Stability of the Lane-Emden Solution for the Viscous Gaseous Star Problem	The Mathematical Problem on the Fluid Dynamics and Related Topics	2016	No	Yes	No
Oct, 2016 Dalian, China	Global Existence of Weak Solutions to the Barotropic Compressible Navier-Stokes Flows with Degenerate Viscosities	Dalian Workshop on Partial Differential Equations and Mathematical Physics	2016	No	Yes	No
Sept, 2016 Obihiro, Japan	Entropis and Uniqueness of Weak Solutions to The Multi-Dimensional Compressible Euler Systems	International Workshop on Mathematical Science for Nonlinear Phenomena	2016	No	Yes	No
Aug, 2016 Taipei, Taiwan	Nonlinear Asymptotic Stability of the Lane-Emden Solution for the Viscous Gaseous Star Problem	2016 NCTS Workshop on Dynamical Systems	2016	No	Yes	No
Aug, 2016 Beijing, China	On Multi-Dimensional Compressible Navier-Stokes Systems	ICCM 2016	2016	No	Yes	No
Aug, 2016 Beijing, China	Global Existence of Weak Solutions to the Barotropic Compressible Navier-Stokes Flows with Degenerate Viscosities	International Conference on PDEs and Applications	2016	No	Yes	No
Jul, 2016 Beijing, China	Nonlinear Asymptotic Stability of the Lane-Emden Solution for the Viscous Gaseous Star Problem	International Workshop on Nonlinear Partial Differential Equations and Scientific Computating	2016	No	Yes	No
Jul 2016 Harbin, China	Riemann and Shock Waves Theory	第十四屆偏微分方程暑期 <i>壆校</i>	2016	No	Yes	No
Jul 2016 Guangzhou China	On Smooth Transonic Flows And Mixed Type Equations	2016 現代數學與統計學 術論壇二	2016	No	Yes	No
Jun, 2016 Daejeon, Korea	Global Existence of Weak Solutions to the Barotropic Compressible Navier-Stokes Flows with Degenerate Viscosities	International Conference on Navier-Stokes equations and related PDEs	2016	No	Yes	No

May 2016	Global Existence of	Nonlinear PDEs: Theories.	2016	No	Yes	No
Hong Kong	Weak Solutions to	Numerics and Applications				
fing Rong	the Barotropic	rumenes and reprications				
	Compressible					
	Navier-Stokes					
	Flows with					
	Degenerate					
	Viscosities					
May 2016	Global Existence of	Workshop on PDEs and	2016	No	Yes	No
Dalian, China	Weak Solutions to	Applications				
	the Barotropic					
	Compressible					
	Navier-Stokes					
	Flows with					
	Degenerate					
	Viscosities					
May 2016	Open problems for	The Third Youth's	2016	No	Yes	No
Wuhan, China	CNS	Academic Forum on PDEs				
,	(blackboard talk.					
	only cover page is					
	available)					
May 2016	Shock Wave	Joint Workshop and	2016	No	Yes	No
Macau. China	Theory	Strategic meeting				
Apr. 2016	Some Results on	Workshop on Solid and	2016	No	Yes	No
Daeieon Korea	Uniqueness of	Liquid Crystals	2010			
Ducjeon, Rorea	Weak Solutions to	Elquid Orystais				
	Systems of Balance					
	I awe					
Mar. 2016	Entropis and	Workshop on PDFs and	2016	No	Ves	No
Hunon China	Uniqueness of	Geometry Analysis	2010	110	105	110
Tiuliali, Cililia	Week Solutions to	Geometry Analysis				
	The					
	Multi Dimonsional					
	Compressible Euler					
	Compressione Euler					
I 2016	Systems	201 (Winter DDE- E-	2016	No	V	No
Jan, 2010	Weels Solutions to	2016 WINTER PDES FORUM	2010	INO	res	INU
Harbin, China	the Departmention					
	Novier Stalses					
	Flame mildle					
	Flows with Decements					
	Degenerate					
1 2016	Viscosities		2016	N	V	N
Jan, 2016	Uniform Estimates	TAS Focused Program on	2016	INO	Y es	INO
Hong Kong	Un I 11	Computation and				
		Mathematical Problems in				
D 2015	Surface waves	The second secon	2016	N	V	N.
Dec, 2015	Riemann Problem	The legacy of Bernhard	2016	NO	Yes	NO
Sanya, China	and Shock Waves	Riemann after one hundred				
D 0015		and fifty years	2016		••) Y
Dec, 2015	Entropis and	Changjiang PDEs	2016	No	Yes	No
Shanghai,	Uniqueness of	Conference				
China	Weak Solutions to					
	The					
	Multi-Dimensional					
	Compressible Euler					
	Systems					
Dec, 2015	Entropis and	International Conference	2016	No	Yes	No
TSIMF, China	Uniqueness of	on Nonlinear Systems of				
	Weak Solutions to	Fluid Dynamic Equations				
	The	and Applications				
	Multi-Dimensional					
	Compressible Euler					
	Systems					

Dec. 2015	Global Existence of	International Conference in	2016	No	Ves	No
Beijing, China	Weak Solutions to the Barotropic Compressible Navier-Stokes Flows with	Mathematics and its Applications	2010		105	
	Degenerate					
NI 2015	Viscosities		2016	N-	V	N
Florida, USA	Multi-dimensional Compressible Navier-Stokes Systems	Mathematical Theory of Fluid Dynamics	2016	INO	I es	NO
Sept, 2015	Global Existence of	International Conference	2016	No	Yes	No
Wuhan, China	Weak Solutions to the Barotropic Compressible Navier-Stokes Flows with Degenerate Viscosities	on Kinetic Equations and Related Topics				
Sept. 2015	1 On Multi-	XL Summer School on	2016	No	Yes	No
Ravello, Italy	Dimensional Dimensional Compressible Navier-Stokes System with Vacuum And Related Topics 2. On Gases Expanding Into Vacuum 3. Global Existence of Weak Solutions to the Barotropic Compressible Navier-Stokes Flows with Degenerate Viscosities	Mathematical Physics	2010			
Aug, 2015 Fudan, China	Uniform Estimates On Incompressible Surface Waves	International Workshop on Mathematics of Geophysical Flows and Turbulance	2016	No	Yes	No
Aug 2015, Yunnan, China	On Uniqueness of Admissible Weak Solutions to Compressible Euler Systems	The Third West China PDE Conference	2016	No	Yes	No
Aug 2015 Xiamen, China	N-S方程:进展和问 题	2015年全国基础数学研究 生暑期学校	2016	No	Yes	No
Jul 2015 Wuhan, China	N-S方程:进展和问 题	The 13rd Summer School and Workshop on PDEs	2016	No	Yes	No
Jun 2015	Uniform Estimates	Workshop on	2016	No	Vec	No
Dalian, China	On Incompressible Surface Wave	Incompressible Fluids And Applications	2010	110	100	110
May 2015 Rizhao, China	On Uniqueness of Admissible Weak Solutions to Compressible Euler Systems	International Conference on Nonlinear PDEs and its Applications	2016	No	Yes	No
May 2015 Beijing, China	On Uniqueness of Admissible Weak Solutions to Compressible Euler Systems	Workshop on Nonlinear Partial Differential Equations	2016	No	Yes	No

May 2015	Some Basic	2nd Workshop on	2016	No	Yes	No
Xian, China	Problems for N-S	Nonlinear PDEs for Young				
	System	Mathematicians				
April 2015	Nonlinear	Workshop on Mathematical	2016	No	Yes	No
Fujian, China	Asymptotic	Physics and Nonlinear				
	Stability of the	PDEs (On the occasion of				
	Lane-Emden	Professor Boling GUO's				
	Solution for the	80th Birthday)				
	Viscous Gaseous					
	Star Problem					
March 2015	Uniform Estimates	11th Japanese-German	2016	No	Yes	No
Tokyo, Japan	On Incompressible	International Workshop on				
	Surface Wave	Mathematical Fluid				
		Dynamics				
January 2015	Periodic Motions	Fourth Workshop on	2016	No	Yes	No
Tokyo, Japan	for the	Mathematical Analysis on				
	One-Dimensional	Fluid Mechanics and				
	Non-isentropic	Conservation Laws				
	Euler Equations					
January 2015	Periodic Motions	International Conference	2016	No	Yes	No
Jinan, China	for the	on Applied Analysis				
	One-Dimensional					
	Non-isentropic					
	Euler Equations					

10. Student(s) trained (*Please attach a copy of the title page of the thesis.*)

Name	Degree	Date of	Date of thesis submission/
	registered for	registration	graduation
YU Rongfeng (submitted in 2016)	PHD	2011-09-01	2015-06-30
LUO Tianwen (submitted in 2016)	PHD	2012-08-01	2015-07-31
YUAN Yuan (submitted in 2016)	MPHIL	2013-08-01	2015-07-31
YUAN Yuan (attached)	PHD	2015-08-01	2018-07-31
MEI Yu (submitted in 2016)	PHD	2013-08-01	2016-07-31
ZHANG Rong (submitted in 2016)	MPHIL	2014-08-01	2016-07-31
ZHANG Rong (attached)	PHD	2016-08-01	2019-07-31
LYU Wenqi (submitted in 2016)	MPHIL	2014-08-04	2016-07-31
LYU Wenqi (attached)	PHD	2016-08-01	2019-07-31
LIU Xin (attached)	PHD	2014-09-01	2017-08-31
XIAO Yao (attached)	PHD	2014-09-01	2017-08-31
YUAN Hongwei (attached)	MPHIL	2015-08-01	2017-07-31
YUAN Hongwei (not yet graduated)	PHD	2017-08-01	2020-07-31
YUAN Qian (attached)	PHD	2016-08-01	2019-07-31
XIN Jing (attached)	MPHIL	2017-08-01	2019-07-31
YEUNG Chin Ching (attached)	MPHIL	2017-08-01	2019-07-31
CHEN Zhendong (not yet graduated)	MPHIL	2018-08-01	2020-07-31

11. Other impact (e.g. award of patents or prizes, collaboration with other research *institutions, technology transfer, etc.*)

N/A